CW2 - Making Classical Models ( The central enterprise of physics is Making and testing models of physical systems. In Classical Mechanics, Hese models are typically some "equation of motion" [EONI]. An equation of motion describes the evolution of the agents (particles) as the interact with their surroundings a each other. Typically, our EDMs are ordinary differential equations arising from

the model of the interactions. (2)  
Examples you have seen  
From a Newtonia a perspective, we  
have,  

$$F_{ret} = ma = m\tilde{x}$$
  
 $\tilde{x} = dt^2$   
 $F_{ret} = ma = m\tilde{x}$   
 $\tilde{x} = dt^2$   
Such that,  
 $dt^2 = \tilde{m}$   
is the general Edu that describes  
the dynamics of the particle of mass, m.  
Dynamics - the (typically) time evolution of  
the system in greation  
 $Specific Examples$   
1D cases -> falling ball (only g); spring-mass







- Sketch the system, identify the 6 - choose your coordinate system - apply the physics framework => obtain EOMS -> priedict Example: Falling Ball workerds Faire = bv J model choice J D Framework? ty FEasch = mg Newton to start. Fret,y = mg-bv = may Eom: my = mg - bv $y^{\circ} = q = \frac{b}{M}V$ 

Questin: What happens when is=0? 7 ?。  $y = g - \frac{b}{m}v = 0$   $v = \frac{ug}{b}$ terminal velocity = for linear drag Que stion: can we solve this?  $= g - \frac{b}{m} \hat{x} \implies \hat{v} = g - \frac{b}{m} v$ For now let's hack off the drag bit, y = g our simplified Edu  $\frac{dy}{dt^2} = g$  or  $\frac{dv}{dt} = g$  and  $\frac{dy}{dt} = V$ 2nd order ODE 2 15t order ODES This is one of our first techiques for sealing with ODES.



Amesone! But vhat if we weren't sine (?) we could integrate these EOMs directly? Ender the discrete form? Ju ID, d<sup>2</sup>y = Fret > dv = Fret dy = V dt = The + dt = The + dy = V  $\frac{\Delta Y}{\Delta t} = \frac{F_{net}}{M} \qquad \frac{\Delta y}{\Delta t} = V$ small st,  $V(++\Delta+) = V(+) + \mp (+) \Delta + /m$ relocity update "Euler Step" Griven information @ time t, F(+) a V(+) we can predict V (++B+) with bt small. V(++0+) = V(+) + (F(+))m) +



