

You have a physical dipole, $+q$ and $-q$ a finite distance d apart. When can you use the expression:

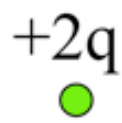
$$V(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \sum_i \frac{q_i}{\mathcal{R}_i}$$

- A. This is an exact expression everywhere.
- B. It's valid for large r
- C. It's valid for small r
- D. No idea...

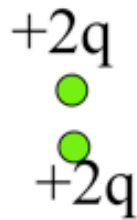
ANNOUNCEMENTS

- Homework 1 due today at 5pm (using gradescope.com)
 - Gradescope will let you turn in until Sunday at 5pm
 - Last two questions turn in on Github
- Quiz #1 - Next Friday
 - Last 25 minutes of class
 - No cheat sheets; all formulas will be provided
 - Solve a Gauss' Law Problem with spherical symmetry
 - Sketch a graph of the resulting electric field

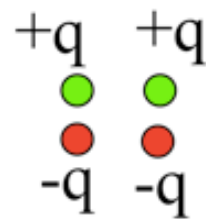
Which charge distributions below produce a potential that looks like $\frac{C}{r^2}$ when you are far away?



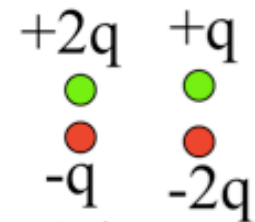
A)



B)



C)

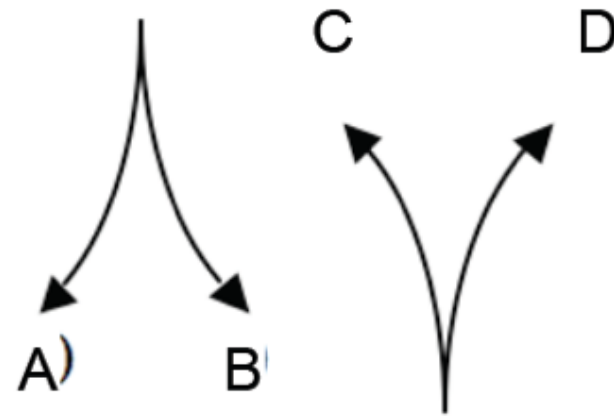
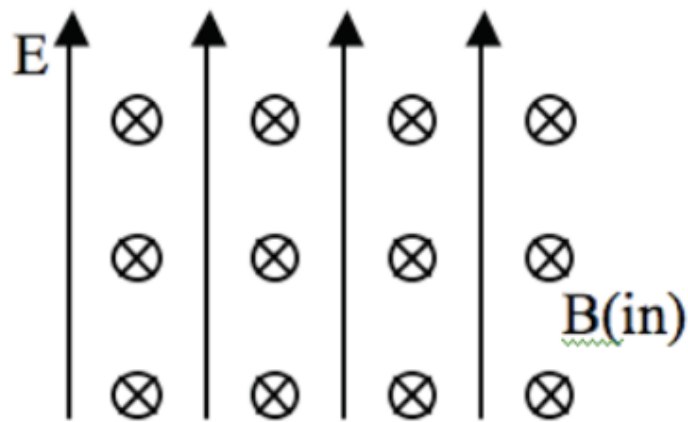


D)

E) None of these, or more than one of these!

(For any which you did not select, how DO they behave at large r ?)

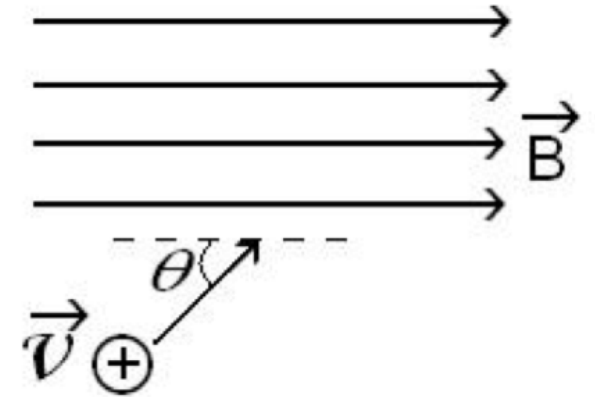
A proton ($q = +e$) is released from rest in a uniform \mathbf{E} and uniform \mathbf{B} . \mathbf{E} points up, \mathbf{B} points into the page. Which of the paths will the proton initially follow?



E. It will remain stationary

A proton (speed v) enters a region of uniform \mathbf{B} . v makes an angle θ with \mathbf{B} .

What is the subsequent path of the proton?



- A. Helical
- B. Straight line
- C. Circular motion, \perp to page. (plane of circle is \perp to \mathbf{B})
- D. Circular motion, \perp to page. (plane of circle at angle θ w.r.t. \mathbf{B})
- E. Impossible. \mathbf{v} should always be \perp to \mathbf{B}

Current I flows down a wire (length L) with a square cross section (side a). If it is uniformly distributed over the entire wire area, what is the magnitude of the volume current density J ?

A. $J = I/a^2$

B. $J = I/a$

C. $J = I/4a$

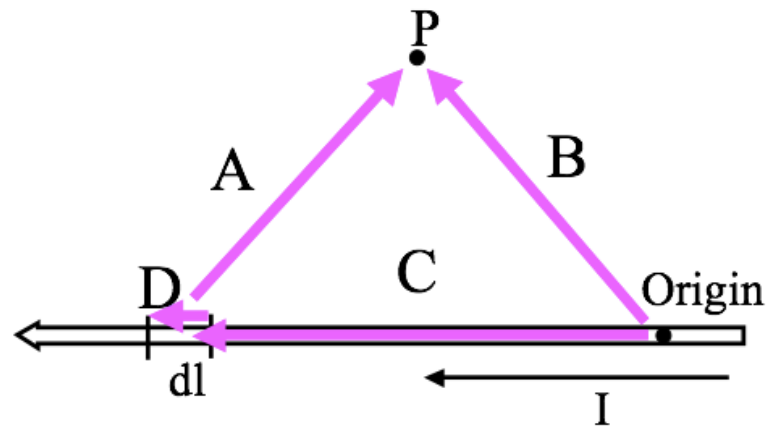
D. $J = a^2 I$

E. None of the above

To find the magnetic field \mathbf{B} at P due to a current-carrying wire we use the Biot-Savart law,

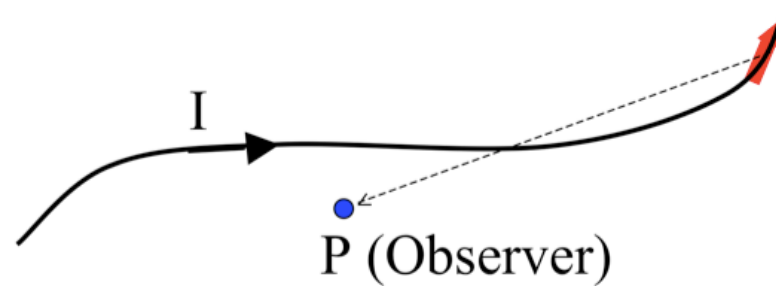
$$\mathbf{B}(\mathbf{r}) = \frac{\mu_0}{4\pi} I \int \frac{d\mathbf{l} \times \hat{\mathcal{R}}}{\mathcal{R}^2}$$

In the figure, with $d\mathbf{l}$ shown, which purple vector best represents \mathcal{R} ?



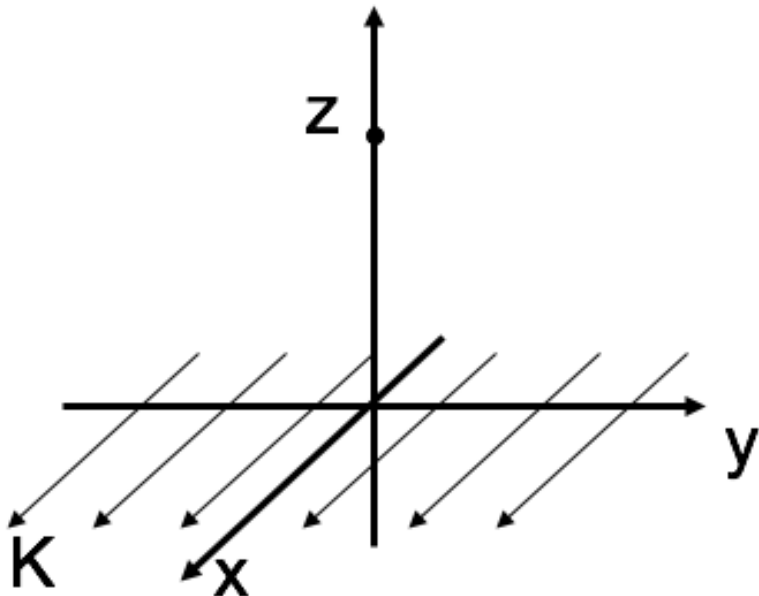
E) None of these!

What do you expect for direction of $\mathbf{B}(P)$? How about direction of $d\mathbf{B}(P)$ generated JUST by the segment of current $d\mathbf{I}$ in red?



- A. $\mathbf{B}(P)$ in plane of page, ditto for $d\mathbf{B}(P, \text{ by red})$
- B. $\mathbf{B}(P)$ into page, $d\mathbf{B}(P, \text{ by red})$ into page
- C. $\mathbf{B}(P)$ into page, $d\mathbf{B}(P, \text{ by red})$ out of page
- D. $\mathbf{B}(P)$ complicated, ditto for $d\mathbf{B}(P, \text{ by red})$
- E. Something else!!

Consider the B-field a distance z from a current sheet (flowing in the $+x$ -direction) in the $z = 0$ plane. The B-field has:

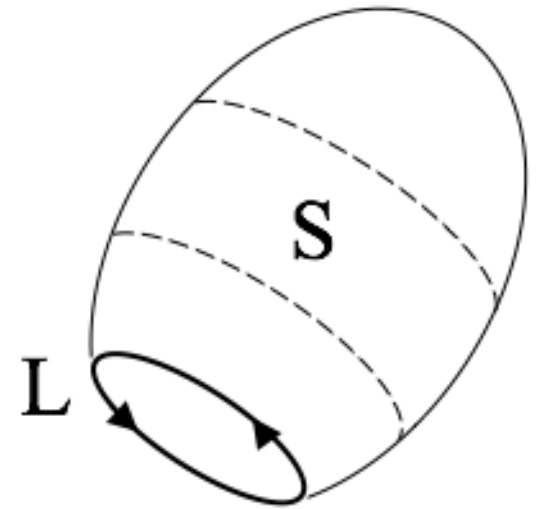


- A. y -component only
- B. z -component only
- C. y and z -components
- D. x , y , and z -components
- E. Other

Stoke's Theorem says that for a surface S bounded by a perimeter L , any vector field \mathbf{B} obeys:

$$\int_S (\nabla \times \mathbf{B}) \cdot d\mathbf{A} = \oint_L \mathbf{B} \cdot d\mathbf{l}$$

Does Stoke's Theorem apply for any surface S bounded by a perimeter L , even this balloon-shaped surface S ?

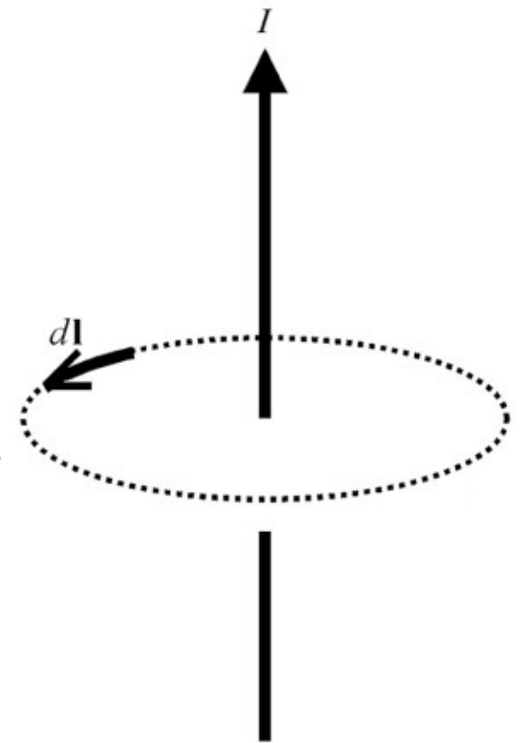


- A. Yes
- B. No
- C. Sometimes

Much like Gauss's Law, Ampere's Law is always true (for magnetostatics), but only useful when there's sufficient symmetry to "pull \mathbf{B} out" of the integral.

So we need to build an argument for what \mathbf{B} looks like and what it can depend on.

For the case of an infinitely long wire, can \mathbf{B} point radially (i.e., in the \hat{s} direction)?

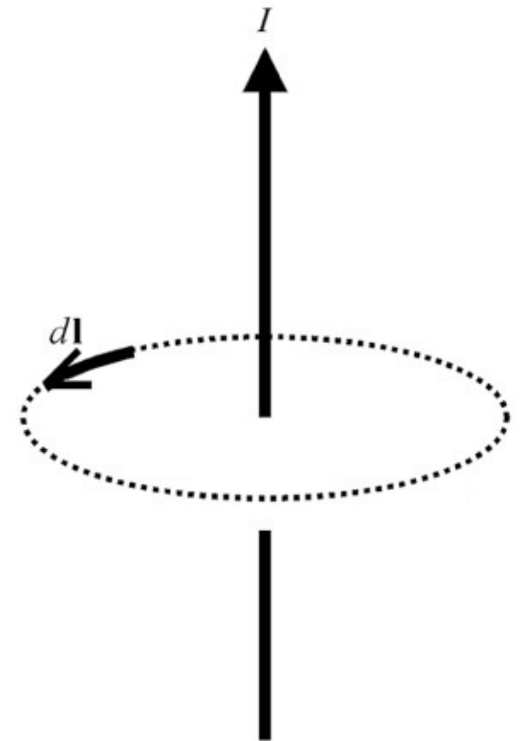


- A. Yes
- B. No
- C. ???

Continuing to build an argument for what \mathbf{B} looks like and what it can depend on.

For the case of an infinitely long wire, can \mathbf{B} depend on z or ϕ ?

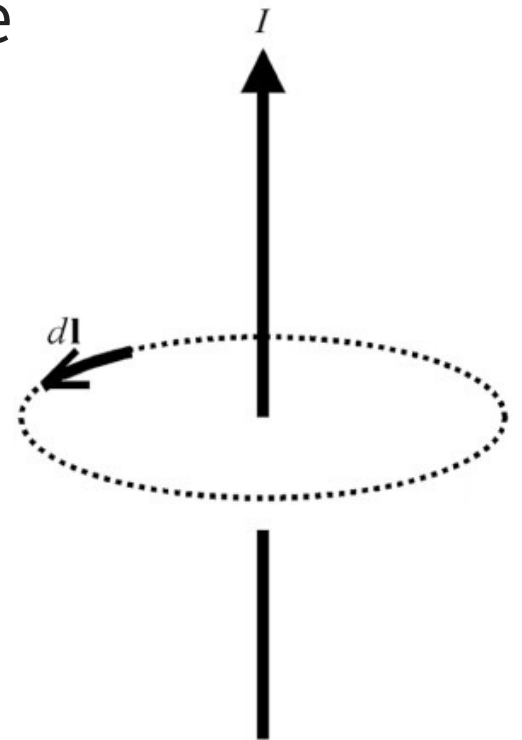
- A. Yes
- B. No
- C. ???



Finalizing the argument for what \mathbf{B} looks like
and what it can depend on.

For the case of an infinitely long wire, can \mathbf{B}
have a \hat{z} component?

- A. Yes
- B. No
- C. ???



Gauss' Law for magnetism, $\nabla \cdot \mathbf{B} = 0$ suggests we can generate a potential for \mathbf{B} . What form should the definition of this potential take (Φ and \mathbf{A} are placeholder scalar and vector functions, respectively)?

A. $\mathbf{B} = \nabla \Phi$

B. $\mathbf{B} = \nabla \times \Phi$

C. $\mathbf{B} = \nabla \cdot \mathbf{A}$

D. $\mathbf{B} = \nabla \times \mathbf{A}$

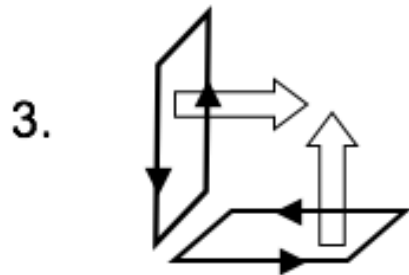
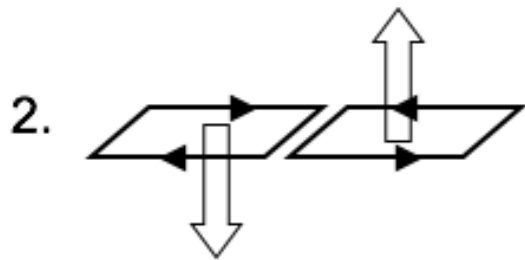
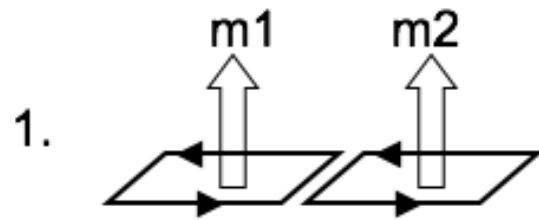
E. Something else?!

We can compute \mathbf{A} using the following integral:

$$\mathbf{A}(\mathbf{r}) = \frac{\mu_0}{4\pi} \int \frac{\mathbf{J}(\mathbf{r}')}{\mathfrak{R}} d\tau'$$

Can you calculate that integral using spherical coordinates?

- A. Yes, no problem
- B. Yes, r' can be in spherical, but \mathbf{J} still needs to be in Cartesian components
- C. No.



Two magnetic dipoles m_1 and m_2 (equal in magnitude) are oriented in three different ways.

Which ways produce a dipole field at large distances?

- A. None of these
- B. All three
- C. 1 only
- D. 1 and 2 only
- E. 1 and 3 only