

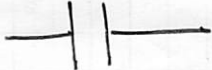


We've studied inductance generally, but now we want see how it might be used more practically. We noticed a few things about self inductance,

$$\phi = LI$$

the emf that is generated when the current changes with time  $I = I(t)$ , is a back emf, which reflects Lenz's Law. The EMF will be produced to fight the change,

$$\mathcal{E} = -\frac{d\phi}{dt} = -L \frac{dI}{dt}$$

In this equation we can see that the inductance,  $L$ , acts like a damping constant on the current,  $I$ . We will study the inductors in circuits so let's remind ourselves of the different circuit elements.

<u>Symbol</u>	<u>Circuit Relation</u>	<u>Geometry</u>	<u>Field</u>
	$Q = CV$ or $I = C dV/dt$	$C = \frac{\epsilon_0 A}{d}$ (parallel plates)	$E = \sigma_b / \epsilon_0$
	$V = IR$	$R = \rho L/A$ (uniform rod)	$J = \sigma E$
	$V = -L \frac{dI}{dt}$	$L = \mu_0 n^2 A * N_{turns}^2$	$B = \mu_0 n I$ or $\Phi_B = LI$

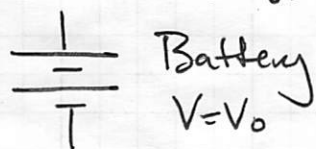
Kirchoff's Laws say,  $\sum_{\text{around any closed loop}} \Delta V = 0$  and  $\sum_{\text{all currents entering any node}} I_{in} = 0$

"Solving a circuit problem" means finding  $I(t)$  &/or  $V(t)$  for all circuit elements.

A few more notes before we get into solving problems,

Sources in circuits can be AC or DC, voltage or current sources,

### Constant Voltage



### Function Generators



AC Voltage Source

$$V = V_0 \sin(\omega t + \delta)$$

$I \uparrow$



AC current source

$$I = I_0 \sin(\omega t + \delta)$$

More Notes:

$$\epsilon_0 = 8.85 \cdot 10^{-12} \frac{\text{farad}}{\text{m}}$$

- real capacitors range from  $\leq 1 \text{ pF}$  to  $> 1 \text{ F}$   
 $10^{-12} \text{ F}$  serious dielectrics

- Typical resistors range from  $< 1 \Omega$  to several  $\text{M}\Omega$   
 $\sim 10^6 \Omega$

$$\mu_0 = 4\pi \cdot 10^{-7} \frac{\text{H}}{\text{m}} \quad (\text{and } L = \frac{\mu_0 N^2 A}{l}) \text{ means}$$

- real life inductors range from  $< 10^{-6} \text{ H}$  to  $\sim 1 \text{ Henry}$

You might be worried about putting an inductor into a circuit and how we define a potential drop across it. This is where  $\Delta V$  & EMF start to get a little confusing. Both are related to energy &/or work. So what we are saying when we say  $\mathcal{E} = -L \frac{dI}{dt}$  is that the work per unit charge for this element is  $-L \frac{dI}{dt}$  so we can use this form in Kirchoff's Law

$$\sum \Delta V = 0,$$