The ODE that describes the R(r) part of our solution is:

$$\frac{d}{dr}\left(r^2\frac{dR}{dr}\right) = l(l+1)R$$

I claim this ODE gives rise to polynomial solutions.

Find a general solution for R(r) in terms of l.

I still have questions about what we are trying to do with separation of variables in spherical coordinates.

- A. Yes, definitely, let's talk about what we are trying to do (briefly).
- B. I have some questions, but I think I got the gist of it. We can move on.
- C. I got it, let's move on.

ANNOUNCEMENTS

- Homework 8 has 2D relaxation problem
 - It is OK to post code on Slack and get help
 - Solution to HW7 (1D relaxation) is linked (you may work from it)
- DC out of town Friday; Rachel will cover

Let's take the Θ ODE term by term starting with l = 0

$$\frac{d}{d\theta} \left(\sin \theta \frac{d\Theta}{d\theta} \right) = 0$$

What are some possible solutions?

Hint: This is not as tricky as it might seem.

$$V(r,\theta) = \sum_{l=0}^{\infty} \left(A_l r^l + \frac{B_l}{r^{l+1}} \right) P_l(\cos\theta)$$

V everywhere on a spherical shell is a given constant, i.e. $V(R, \theta) = V_0$. There are no charges inside the sphere. Which terms do you expect to appear when finding V(inside)?

- A. Many A_l terms (but no B_l 's)
- B. Many B_l terms (but no A_l 's)
- C. Just A_0
- D. Just B_0
- E. Something else!

The general solution for the electric potential in spherical coordinates with azimuthal symmetry (no ϕ dependence) is:

$$V(r,\theta) = \sum_{l=0}^{\infty} \left(A_l r^l + \frac{B_l}{r^{l+1}} \right) P_l(\cos\theta)$$

Consider a metal sphere (constant potential in and on the sphere, remember). Which terms in the sum vanish outside the sphere? (Recall: $V \rightarrow 0$ as $r \rightarrow \infty$)

A. All the A_l 's B. All the A_l 's except A_0 C. All the B_l 's D. All the B_l 's except B_0 E. Something else

Given
$$V_0(\theta) = \sum_l C_l P_l(\cos \theta)$$
, we want to get to the integral:

$$\int_{-1}^{+1} P_l(u) P_m(u) du = \frac{2}{2+1} \text{ (for } l = m\text{)}$$

we can do this by multiplying both sides by:

A. $P_m(\cos \theta)$ B. $P_m(\sin \theta)$ C. $P_m(\cos \theta) \sin \theta$ D. $P_m(\sin \theta) \cos \theta$ E. $P_m(\sin \theta) \sin \theta$